STUDIES ON AN IMPROVED COMPACT PHYSICS PACKAGE FOR RUBIDIUM STANDARDS

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Abstract

We present a compact laser-pumped rubidium frequency standard with a short-term frequency stability of \(6 \times 10^{-13} \tau^{-1/2}\) and having a fundamental shot-noise limit below \(8 \times 10^{-14} \tau^{-1/2}\). Our clock employs the physics package with a 25 mm diameter buffer-gas cell inside a compact microwave cavity, a newly developed laser head with integrated acousto-optical modulator to minimize the Light Shift effect, and a low-noise microwave synthesizer. This work paves the way for realization of clock stabilities \(\sigma(\varphi) \times 1 \times 10^{-13} \tau^{-1/2}\) with a compact standard.

INTRODUCTION

Rubidium standards have become the backbone for various applications in everyday life, such as space navigation and telecommunications [1]. Traditional rubidium standards have been using discharge lamps for optical pumping. Since last few decades, laser-pumped rubidium standards have been a subject of interest to develop the Rb standards aiming to attain better stabilities [2]. Constantly improving availability of lasers in the interested optical-pumping wavelengths of rubidium have made this technology possible. A compact, laser-pumped clock using an Extended Cavity Diode Laser (ECDL) has been already demonstrated with a short-term stability of \(3 \times 10^{-12} \tau^{1/2}\) [3]. Recently, Distributed-Feedback (DFB) laser sources have become commercially available, with advantages of being robust and compact. First studies on important issues concerning ageing, lifetime, etc., have been done on 894 nm DFB lasers [4]. Today, the best frequency stability reported for a vapor cell passive Rb frequency standard using a laser diode is \(3 \times 10^{-13} \tau^{-1/2}\) [2,5].

In this communication we present a 25 mm diameter buffer-gas (B-G) cell in a magnetron [6] type microwave resonator physics package (PP). Compared with our previous clock realization [7], a bigger cell dimension allows interrogating a higher number of atoms with the standing microwave field inside
the cavity. This leads to improved contrast and reduced linewidth of the clock signal, and finally results in a better signal-to-noise ratio.

We also present a newly developed compact DFB laser head with an Acousto-Optical-Modulator (AOM) integrated into the laser head [8]. The AOM is used to detune the laser frequency to reduce the light-shift effect on the clock frequency.

The clock-loop is closed using a low-noise microwave synthesizer. Measured Allan deviation plots of our clock are presented and are compared to the predicted shot-noise and signal-to-noise limits. Finally, we conclude with a comparison of the clock stabilities obtained with different Rb cells using buffer gas and wall-coating [9] for the PPs, along with possible future prospects.

**CLOCK GOAL AND DESIGN REQUIREMENTS**

Our clock goal is to achieve the stability of $< 1 \times 10^{-12} \tau^{1/2}$ between 1 to 4000 s and $< 1 \times 10^{-14}$ (drift removed) up to 1 day. As a first step, we focus ourselves to only short-term stability of $< 1 \times 10^{-12} \tau^{1/2}$ between 1 to 100 s. After the integration time of 100 s, thermal effects start to dominate in our current setup, and improvements on this part are envisaged for the next stages of the experiment.

The clock design requirements concern the three main subsystems: (i) a stabilized laser source, (ii) physics package (PP), and (iii) microwave Local Oscillator (LO) source, to interrogate the atoms that resonate at clock frequency. Each subsystem design requirement to reach the clock goal is explained below.

(i) **Laser source:** A collimated laser beam with a wavelength of 780 nm (Rb D2 line) and output power of at least few tens of microwatts (after passing through the optical components) is required to optically pump the $^{87}$Rb atoms into one of the hyperfine ground states. The linewidth of the laser should be in few MHz range in order to resolve the narrow sub-Doppler saturated-absorption transitions used for laser stabilization. This feature is required for stabilizing the laser frequency by locking to one of the sub-Doppler transitions. The Relative Intensity Noise (RIN) and FM noise should be $< 10^{11}$ Hz$^{-1}$ and $< 10$ kHz/$\sqrt{\text{Hz}}$, respectively, to reach the clock goal of $< 1 \times 10^{-12} \tau^{1/2}$. Desired power stability of the laser in order to avoid the clock drift is within 0.1 %/day, at fixed environmental conditions. Finally, the frequency stability of the laser should be $< 1 \times 10^{-11} \tau^{1/2} (1 - 4000 \text{ s})$ and $\leq 3 \times 10^{-13}$ for 4000 s to 1 day.

(ii) **The Physics Package (PP):** The requirements with PP are to achieve a double-resonance (DR) signal with a linewidth of $< 1$ kHz and a good discriminator slope, typically $> 1$ nA/Hz. The noise of the laser after passing through PP, measured at the detector output, should be close to 5 pA/$\sqrt{\text{Hz}}$. The Rb cell should exhibit a temperature coefficient of $< 1 \times 10^{11} /\text{C}$ at its operating temperature, which is important for obtaining the envisaged medium-term and long-term stabilities. This temperature coefficient is obtained by an optimized buffer-gas mixture of argon and nitrogen in the Rb cell. Magnetic shields are required around the Rb cell to have $< 10^{13} /\text{G}$ sensitivity.

(iii) **Local Oscillator (LO):** A synthesizer which can generate a stable 6.835 GHz of microwave frequency and a power output of $\sim 10$ dBm is required, though the required power level can be reduced significantly at the clock operational stage. A typical tuning range of 2 MHz would be ideal, with a step resolution of $< 1$ Hz. An important factor here is the phase noise.

In principle, the phase-noise limited short-term stability in a quasi-static model for the square wave modulation with frequency $f_n$ can be written in terms of spectral density $S_\phi(f)$ as [10]
$f_n$ is typically in the range of 100-300 Hz. For our clock, referred to a 10 MHz carrier, a phase noise of $\leq -137$ dBrad$^2$/Hz @ 100 Hz and $\leq -147$ dBrad$^2$/Hz @ $f_n \geq 1$ kHz is required.

**EXPERIMENTAL SETUP: LASER HEAD AND PHYSICS PACKAGE**

Our double-resonance experimental clock setup is shown in the schematics of

Figure 1. A laser source is implemented to optically pump the Rb atoms. A first feedback loop is implemented in order to lock the laser frequency to a desired sub-Doppler transition obtained from the reference spectroscopy cell. A second feedback loop is used to lock the microwave frequency of the LO to the $^{87}$Rb microwave clock transition ($5^2S_{1/2} \left| F_g = 1, 0 \right\rangle \rightarrow \left| F_g = 2, 0 \right\rangle$).

![Schematic of the experimental setup](image)

Figure 1. Schematics of the experimental setup are shown with a DFB laser stabilized by a feedback loop. The Acousto-Optical-Modulator (AOM) helps in detuning the laser frequency. Further, the expanded laser beam interrogates the $^{87}$Rb atoms inside the magnetron cavity that resonates around 6.835 GHz. The absorption signal captured on a photo detector (PD) is fed back to the synthesizer to form a clock loop.

**STABILIZED AOM LASER HEAD**

The laser head contains mainly three subcomponents: (i) A DFB laser as a source that gives the output at 780 nm, to interrogate the $^{87}$Rb atoms at D2 transition, (ii) an AOM to shift the laser frequency, (iii) a reference cell saturated-absorption setup. A photograph of the laser head is shown in Figure 2.
A beam-splitter divides the beam just after the output from the laser source. One part of the beam is directly taken as the output to interrogate the atoms in the PP and the other part is used to stabilize the laser frequency [11]. The stabilization beam is made to pass through the AOM, either in single-pass or double-pass configuration, depending on the frequency detuning required. The detuned beam is used to obtain a saturated-absorption signal by passing through a reference rubidium cell. The resulting sub-Doppler absorption signal is used as feedback to the control electronics of the laser head. The key characteristics of the laser head are shown in Table 1 below.

<table>
<thead>
<tr>
<th>Linewidth [MHz]</th>
<th>Relative Intensity Noise (RIN) [Hz⁻¹] @ 300 Hz</th>
<th>FM noise [kHz/√Hz] @ 300 Hz</th>
<th>Side-Mode Suppression Ratio (SMSR) [dB]</th>
<th>Frequency stability from beat measurement @ 1-300 s [τ⁻¹/₂]</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt; 5</td>
<td>5×10⁻¹⁴</td>
<td>7</td>
<td>&gt; 40</td>
<td>&lt; 9×10⁻¹²</td>
</tr>
</tbody>
</table>

**PHYSICS PACKAGE (PP)**

A cell filled with $^{87}$Rb atoms and a buffer-gas mixture of argon and nitrogen is shown in Figure 3(a). The cell has a diameter of 25 mm and a stem in which the metallic rubidium is stored. A controlled temperature on the stem ensures the vapor content of Rb inside the cell volume. This cell is mounted inside a newly developed magnetron-type cavity (cf. Figure 3(b)).
Figure 3. (a) Buffer-gas cell (Ar/N₂ mixture) with support cap. (b) Assembled & tuned magnetron-type cavity with the cell. External diameter of the cavity is 40 mm.

Figure 4. Fully assembled PP shown. Two µ-metal magnetic shieldings cover the tuned cavity.

The tuned cavity along with the cell is placed inside a holder, on which is wound a C-field coil for splitting the degenerate ground-state hyperfine levels to Zeeman sub-levels, of which we are interested only in the clock transition. This whole cavity assembly is covered by two µ-metal magnetic shields, which have a measured longitudinal shielding factor of 3067. Two separate heaters are implemented: one for cell volume and another one for the cell stem. The respective temperatures are sensed using NTC resistors. A telescope assembly at the input end of the PP expands the laser beam to the cell dimension, which is useful to interrogate the full cell volume for better signal contrast. At the rear end of the PP, a focusing lens assembly focuses the light onto the photodetector. The fully assembled PP with above explained design is shown in Figure 4.
DOUBLE-RESONANCE (DR) AND LIGHT-SHIFT (LS)

DR SIGNAL

Double-Resonance (DR) involves two resonant electromagnetic fields: first, the optical-pumping resonant field (D2 line, 5S_{1/2} → 5P_{3/2}) provided by the laser, to pump all the atoms to one of the atomic ground states; and second, a microwave field for driving the ground-state hyperfine transition at ~ 6.835 GHz, which is applied to the atoms using the microwave cavity. A typical DR signal of the clock transition from our clock setup is shown in Figure 5. Experimental parameters for the experiment were a cell temperature around 50 °C, a laser power to the PP of 120 µW, and the laser frequency locked to the F_g = 2 to F_e = 2-3 cross-over resonance in the ^87Rb D2 line. A static magnetic C-field of 174 mG was applied in the direction of the optical path, to split the Zeeman sub-levels and detect only the m_f = 0→0, “clock transition.”

![Graph](image)

Figure 5. Double-resonance signal.

The DR signal has a high contrast of 19% and a narrow linewidth of 548 Hz, resulting in an error signal with an excellent discriminator slope of 1.5nA/Hz. Note that with this PP linewidths as low as 288 Hz were measured, and even lower linewidths may be achieved when reducing further the optical and/or microwave power. The estimated short-term stability based on the above DR signal is explained in detail in Table 2.

LIGHT SHIFT, AND ITS REDUCTION BY DETUNING METHOD

The AC Stark shift, commonly known as Light Shift, of the electromagnetic field on the clock transition is a basic limitation usually encountered in Rb clocks when in continuous wave (CW) operation. It arises due to the light field driving virtual transitions in the atom, and in this sense is fundamentally related to the Lamb shift which arises due to an atom’s interaction with the vacuum field [1]. The light shift can be approximated as [3].

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where $v_L$ is the pump-laser frequency, $\Gamma$ is the width of the approximated Lorentzian signal centered at the pumped optical atomic transition $v_0$, and $I$ is the intensity of the light. The intensity light-shift coefficient slope $\alpha$ can be written as $\alpha = \frac{\partial \Delta v_{LS}}{\partial I}$ at a given laser frequency. The AOM integrated laser head is used to minimize $\alpha$ by controlled detuning of the laser to a frequency $v_L \approx v_0$ where $\alpha$ is small [12]. Figure 6 shows both the undetuned LS coefficient (measured with the laser frequency directly stabilized to the Rb saturated absorption lines) and the reduced value of light shift $\alpha$ obtained by controlled detuning of the laser frequency using the AOM.

By adjusting the laser frequency sent to the PP using the AOM, we obtain $\alpha = 2.7 \text{ mHz}/\mu\text{W}$. This is reduced by a factor of 37 compared to the lowest LS coefficient value of $\alpha = 0.1 \text{ Hz}/\mu\text{W}$, which is obtained without the AOM (i.e. with the pump-light frequency stabilized directly to one of the reference saturated-absorption lines). By finely adjusting the detuning frequency, one can reduced the LS coefficient value to be even less.

\[
\Delta v_{LS} \sim \frac{1}{(v_L-v_0)^2+\Gamma^2}
\]  

(2)

Figure 6. Light Shift without AOM for locking to different $^{87}\text{Rb}$-D2 transitions, and reduced LS effect with the AOM laser head are shown.

**CLOCK LOOP AND MICROWAVE SYNTHESISER**

The design was finalized based on the electronics of the Coherent Population Trapping maser [13] and of the Pulsed Optically Pumped (POP) rubidium clock developed by IEN, Torino. In particular, the synthesis chain scheme is similar to the one of the CPT maser, while the lock-in scheme is taken from the POP clock.

The Local Oscillator (LO) interrogates the atoms by means of the synthesis chain. The signal coming from the photodiode is amplified by the trans-impedance amplifier (TI), acquired by an analog-to-digital
converter (ADC) and then processed by a programmable logic device (PLD) that implements the lock-in and the integrator blocks. The loop gain, and consequently the loop bandwidth, can be adjusted by changing a multiplicative constant. All the parameters involved are set via a computer user interface. With respect to the CPT Maser, the signal-to-noise ratio at 1 s of the ADC is improved from 100 dB to 120 dB by increasing the sampling frequency (from 100 kHz to 10 MHz) and the noise bandwidth (from 10 kHz to 1 MHz). The lock-in scheme allows a first-order rejection of the electronic offset, drift, and flicker noise, leading a more stable long-term behavior. The integrator, also digitally implemented, does not introduce any offset and any other kind of long-term fluctuations. The 16-bit digital-to-analog converter (DAC) allows a frequency resolution better than $10^{-12}$ and an electronic tuning of the OCXO of about $10^7$.

Figure 7. Block diagram of LO electronics.

The first frequency multiplication stages are designed to multiply the 10 MHz signal up to 180 MHz. This frequency is suitable for direct multiplication in the microwave range by a Step-Recovery Diode (SRD) that produces a continuous comb of spectral components separated by 180 MHz. The required components at 7.02 GHz are filtered out by coaxial filters and are cleaned by residual nearby components of the multiplication process by using a Yttrium-Iron-Garnet oscillator (YIG). As shown in Figure 8, the 7.02 GHz signal is mixed with the 185.3 MHz one inside the YIG Phase Lock Loop (PLL) in order to refer the YIG to the quartz oscillator. The 183.7 MHz is obtained as a sum of 180 MHz and 5.3 MHz coming from a Direct Digital Synthesizer (DDS), which realizes the fine tuning of the synthesis chain. Moreover, the DDS is also used for phase/frequency modulation purposes.
A picture of LO electronics with the loop electronics and synthesis chain is shown in Figure 9 below.

Two identical synthesis chains have been compared using the homodyne technique and the result has been referred to a 10 MHz carrier. It has a flicker level of $-124$ dB rad$^2$/Hz and a noise floor of $-154$ dB rad$^2$/Hz.
CLOCK STABILITY

Integrating all the three subsystems; the laser head, the physics package, and the microwave synthesizer, the clock loop is closed as shown in Figure 7. We measure the clock stability by comparing our clock signal (10 MHz quartz) to that of an active hydrogen maser. Using the DR signal of Figure 5 and the measured clock-loop noise, we estimate the short-term stability limit for our clock to be \( < 6 \times 10^{-13} \tau^{-1/2} \), as detailed in Table 2.

Table 1. Estimation of short-term stability with DR signal and measured clock-loop noise.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>DR Linewidth [Hz]</td>
<td>548</td>
</tr>
<tr>
<td>Contrast [%]</td>
<td>19</td>
</tr>
<tr>
<td>Discriminator slope [A/Hz]</td>
<td>(1.5 \times 10^{-9})</td>
</tr>
<tr>
<td>Total measured detection noise [A/√Hz]</td>
<td>(8.5 \times 10^{12})</td>
</tr>
<tr>
<td>(laser noise + μ-wave noise + lock-in loop noise etc.)</td>
<td></td>
</tr>
<tr>
<td>Signal-to-noise (S/N) short-term stability ([\tau^{1/2}])</td>
<td>(5.9 \times 10^{13})</td>
</tr>
<tr>
<td>Shot-noise estimated stability ([\tau^{1/2}])</td>
<td>(7.8 \times 10^{14})</td>
</tr>
</tbody>
</table>
The above estimated shot-noise limit and the signal-to-noise (S/N) limit are plotted along with the measured clock stability of $8 \times 10^{-13} \tau^{-1/2}$ in Figure 11, in terms of Allan deviation. The measured Allan plot is also shown for LS compensation implemented by using the AOM detuning method, which gives $6 \times 10^{-13} \tau^{-1/2}$. The estimated S/N-limit and measured clock stabilities are in close agreement with each other. Furthermore, we find a shot-noise limit of $< 8 \times 10^{-14} \tau^{-1/2}$, which makes it possible to envisage a future realization of a Rb clock with a stability $< 1 \times 10^{-13} \tau^{-1/2}$.

Figure 11. Allan deviation measurements, also showing the improvement in stability by LS reduction.

**SHORT-TERM STABILITY COMPARISON WITH DIFFERENT CELLS**

Here we compare the short-term stabilities for cells with 14 mm and 25 mm diameter, to give insight on the impact of the cell dimension. The 25 mm cell shows a better shot-noise limit of $7.8 \times 10^{-14} \tau^{-1/2}$, in comparison to $2.9 \times 10^{-13} \tau^{-1/2}$ when using a 14 mm cell [7].
CONCLUSIONS AND FUTURE PROSPECTS

A new PP for Rb clocks, based on a magnetron-type microwave cavity accepting a cell of 25 mm diameter was presented, which is bigger than in our previous realizations (14 mm) [7]. The measured short-term stability is $6 \times 10^{-13} \tau^{-1/2}$, and the shot-noise limit of less than $8 \times 10^{-14} \tau^{-1/2}$ opens the way for $\leq 1 \times 10^{-13} \tau^{-1/2}$ stability from a compact gas-cell clock. The design of a suitable microwave source and loop electronics was presented. Reduction of the noise from LO and loop electronics will be important to achieve the above mentioned stability of $\leq 1 \times 10^{-13} \tau^{-1/2}$. Improvement of clock stability is demonstrated by fine-tuning the intensity light shift using an AOM integrated laser head developed at LTF. Finally, the 14 mm and 25 mm PPs are compared, and show improved stability for the PP using the bigger cells.

As an alternative to buffer-gas cells, long relaxation times up to few seconds [14] can be obtained by using surface coatings in the Rb cell technology. Such wall-coated cells can be good candidates for use in Rb standards. In addition, a combination of buffer gas and wall-coated technologies could also help to make better clocks in the future. An initial study on integrating these two technologies was recently published by S. Knappe and H. Robinson [15]. Use of these cells is not only restricted to clocks, but they can also be potential candidates in sensitive magnetometers and other applications where a narrow line-width signal is crucial.

ACKNOWLEDGMENTS

We acknowledge support and funding by the European Space Agency (ESA) (contracts 19392/05/NL/CP and 21504/08/NL/GLC), the Swiss National Science Foundation (grant 200020-105624, CRSI20-122693/1) and Swiss Space Office (SSO). We thank the contributions from our colleagues, M. Pellaton (in particular for providing the Rb cell), F. Gruet, P. Scherler, and M. Durrenberger. We also thank H. Schweda for the support on cavity work.
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